Holy Cross Catholic Primary School



## **Calculation Policy- Upper Key Stage Two**

## **KEY STAGE 2**

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

Key language: decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage. Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods. Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.	Multiplication and division: Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers. Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000. Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions. Multiplication and division of decimals are also introduced and refined in Year 6.	<b>Fractions:</b> Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them. Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic. Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.
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	Year 5			
	Concrete	Pictorial	Abstract	
Year 5 Addition				
Column addition with whole numbers	Use place value equipment to represent additions. Add a row of counters onto the place value grid to show 15,735 + 4,012.	Represent additions, using place value equipment on a place value grid alongside written methods. $\underbrace{\frac{TTh}{0} + \frac{Th}{0} + \frac{T}{0} + $	Use column addition, including exchanges.	
Representing additions		Bar models represent addition of two or more numbers in the context of problem solving. $\begin{array}{c c} & & & \\ \hline flq,57q & fld,725 \\ \hline flq,57q & fld,725 \\ \hline flq,57q & fld,725 \\ \hline \\ Jen & fld,00 \\ \hline \\ Holly & fld,00 \\ \hline \\ fld,050 \\ \hline \\ \hline \\ \frac{Th}{2} \frac{H}{6} \frac{T}{0} \frac{Th}{2} \frac{H}{6} \frac{T}{0} \frac{Th}{2} \frac{H}{6} \frac{T}{0} \frac{T}{0} \frac{Th}{2} \frac{H}{6} \frac{T}{0} \frac{T}{0} \frac{Th}{2} \frac{H}{6} \frac{T}{0} \frac{T}{0} \frac{Th}{2} \frac{H}{6} \frac{T}{0} \frac{T}{0$	Use approximation to check whether answers are reasonable. $\frac{TTh Th H T O}{2 3 4 0 5} \qquad \frac{TTh Th H T O}{2 3 4 0 5} + \frac{7 8 9 2}{2 0 2 9 7} + \frac{7 8 9 2}{3 1 2 9 7} + \frac{7 8 9 2}{3 1 2 9 7}$ <i>I will use 23,000 + 8,000 to check.</i>	
Adding tenths	Link measure with addition of decimals. <i>Two lengths of fencing are 0.6 m and</i> <i>0.2 m.</i> <i>How long are they when added together?</i>	Use a bar model with a number line to add tenths.	Understand the link with adding fractions. $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$	

	0.6 m 0.2 m	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	6 tenths + 2 tenths = 8 tenths 0·6 + 0·2 = 0·8
Adding decimals using column addition	Use place value equipment to represent additions. Show 0.23 + 0.45 using place value counters.	Use place value equipment on a place value grid to represent additions. Represent exchange where necessary. $\underbrace{\bigcirc & \hline Tth & Hth}_{\hline 0 & 0 & 2 \\ + & 0 & 3 & 3 \\ \hline 1 & 2 & 5 \\ \hline 1 & \hline 1 & \hline 1 & 2 & 5 \\ \hline 1 & \hline 1 & \hline 1 & 1 \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & 1 \\ \hline 0 & \hline 1 & 1 & Hth \\ \hline 0 & \hline 1 & 1 & 1 \\ \hline 1 & \hline 1 & 1 \\ \hline 1 & \hline 1 & 1 \\ \hline 1 & \hline 1 & 1 \\ \hline 1 & $	Add using a column method, ensuring that children understand the link with place value. $\frac{O \cdot Tth Hth}{0 \cdot 2 \cdot 3}$ + $\frac{O \cdot 4 \cdot 5}{0 \cdot 6 \cdot 8}$ Include exchange where required, alongside an understanding of place value. $\frac{O \cdot Tth Hth}{0 \cdot 9 \cdot 2}$ + $\frac{O \cdot 3 \cdot 3}{1 \cdot 2 \cdot 5}$ Include additions where the numbers of decimal places are different. 3.4 + 0.65 = ? $\frac{O \cdot Tth Hth}{3 \cdot 4 \cdot 0}$ + $\frac{O \cdot 6 \cdot 5}{-1}$
Year 5 Subtraction			
Column subtraction with whole numbers	Use place value equipment to understand where exchanges are required. 2,250 – 1,070	Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required.	Use column subtraction methods with exchange where required.

		$15,735 - 2,582 = 13,153$ $\begin{array}{c c c c c c c c c c c c c c c c c c c $	$\frac{\text{TTh Th H T O}}{\frac{56}{9} \frac{12}{9} 0 9 7}$ $-\frac{18534}{43563}$ $62,097 - 18,534 = 43,563$
Checking strategies and representing subtractions		Bar models represent subtractions in problem contexts, including 'find the difference'. Athletics Stadium 75,450 Hockey Centre $42,300$ Velodrome $15,735$ ?	Children can explain the mistake made when the columns have not been ordered correctly. $ \begin{array}{c} \hline \\ \hline $
Choosing efficient methods			To subtract two large numbers that are close, children find the difference by counting on. 2,002 - 1,995 = ? Use addition to check subtractions. <i>I calculated 7,546 - 2,355 = 5,191.</i> <i>I will check using the inverse.</i>
Subtracting	Explore complements to a whole number by	Use a place value grid to represent the	Use column subtraction, with an

decimals	working in the context of length. 0.49  m 1  m -  m =  m 1 - 0.49 = ?	stages of column subtraction, including exchanges where required. $5 \cdot 74 - 2 \cdot 25 = ?$ $\bigcirc$ <t< th=""><th>understanding of place value, including subtracting numbers with different numbers of decimal places. <math display="block">3 \cdot 921 - 3 \cdot 75 = ?</math> <math display="block">\frac{0 \cdot \text{Tth } \text{Hth } \text{Thth}}{3 \cdot 9 \cdot 2 \cdot 1}</math> <math display="block">- \frac{3 \cdot 7 \cdot 5 \cdot 0}{\cdot 2 \cdot 1}</math></br></th></t<>	understanding of place value, including subtracting numbers with different numbers of decimal places. 
Year 5 Multiplication			
Understanding factors	Use cubes or counters to explore the meaning of 'square numbers'. 25 is a square number because it is made from 5 rows of 5. Use cubes to explore cube numbers.	Use images to explore examples and non- examples of square numbers. $8 \times 8 = 64$ $8^2 = 64$	Understand the pattern of square numbers in the multiplication tables. Use a multiplication grid to circle each square number. Can children spot a pattern?

	8 is a cube number.	12 is not a square number, because you cannot multiply a whole number by itself to make 12.	
Multiplying by 10, 100 and 1,000	Use place value equipment to multiply by 10, 100 and 1,000 by unitising. $\frac{4 \times 1 = 4 \text{ ones} = 4}{4 \times 10 = 4 \text{ tens} = 40}$	Understand the effect of repeated multiplication by 10.	Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000. $\begin{array}{c c} H & T & O \\ \hline I & 7 \\ \hline 17 \times 10 = 170 \\ \end{array}$
Multiplying by	Use place value equipment to explore	Use place value equipment to represent	$17 \times 100 = 17 \times 10 \times 10 = 1,700$ $17 \times 1,000 = 17 \times 10 \times 10 \times 10 = 17,000$ Use known facts and unitising to multiply.
multiples of 10, 100 and 1,000	multiplying by unitising.	how to multiply by multiples of 10, 100 and 1,000. $4 \times 3 = 12$ $4 \times 300 = 1,200$ $6 \times 4 = 24$ $6 \times 400 = 2,400$	$5 \times 4 = 20$ $5 \times 40 = 200$ $5 \times 400 = 2,000$ $5 \times 4,000 - 20,000$ $5,000 \times 4 = 20,000$
Multiplying up to 4-digit numbers by a	Explore how to use partitioning to multiply efficiently.	Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.	Use an area model and then add the parts.

single digit	8 × 17 = ?		100 60 3
0 0		Н Т О	5 100 × 5 = 500 60 × 5 = 300 3 × 5 = 15
			Use a column multiplication, including any
			required exchanges.
			I 3 6 × 6
	8 × 10 = 80 8 × 7 = 56		<u>8   6</u> 2 3
	80 + 56 = 136		
	So, 8 × 17 = 136		
Multiplying 2-	Partition one number into 10s and 1s, then	Use an area model and add the parts.	Use column multiplication, ensuring
digit numbers by 2-digit numbers	add the parts. $23 \times 15 = ?$	28 × 15 = ?	understanding of place value at each stage.
		20 m 8 m H T O 2 0 0	× 27
		$10 \text{ m} \qquad 20 \times 10 = 200 \text{ m}^2 \qquad 8 \times 10 = 80 \text{ m}^2 \qquad 1  0  0 \\ 8  0 \qquad 0$	2 3 <sub>2</sub> 8 34 × 7
	10 × 15 = 150 10 × 15 = 150	5 m $20 \times 5 = 100 \text{ m}^2$ $8 \times 5 = 40 \text{ m}^2$ $+ \frac{4 \ 0}{4 \ 2 \ 0}$	3 4
	H T O 1 5 0 1 5 0	28 × 15 = 420	$\times \frac{27}{23_28}$ 34 × 7
	$3 \times 15 = 45$ + $4 5$ There are 345 bottles of milk in total. $3 4 5$		$\frac{680}{34 \times 20}$ 34 × 20
	23 × 15 = 345		3 4 × 2 7
			$23_{2}8$ 34 × 7 6 8 0 34 × 20
			$\frac{0}{9} \frac{1}{1} \frac{8}{3} \frac{34 \times 20}{34 \times 27}$
Multiplying up		Use the area model then add the parts.	Use column multiplication, ensuring

to 4-digits by 2-digits		100   40   3   Th H T O  2   4   0   2   0   0   8   0   3   0   0	understanding of place value at each stage. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Multiplying decimals by 10, 100 and	Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.	Represent multiplication by 10 as exchange on a place value grid.	Understand how this exchange is represented on a place value chart.

1,000		$0 \cdot 14 \times 10 = 1 \cdot 4$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $
Year 5 Division			
Understanding factors and prime numbers	Use equipment to explore the factors of a given number.	Understand that prime numbers are numbers with exactly two factors.	Understand how to recognise prime and composite numbers.
	24 ÷ 3 = 8 24 ÷ 8 = 3 8 and 3 are factors of 24 because they divide 24 exactly. 24 ÷ 5 = 4 remainder 4. 5 is not a factor of 24 because there is a remainder.	13 ÷ 1 = 13 13 ÷ 2 = 6 r 1 13 ÷ 4 = 4 r 1 1 and 13 are the only factors of 13. 13 is a prime number.	I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder. I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33. I know that 1 is not a prime number, as it has only 1 factor.
Understanding inverse operations and the link with	Use equipment to group and share and to explore the calculations that are present.	Represent multiplicative relationships and explore the families of division facts.	Represent the different multiplicative relationships to solve problems requiring inverse operations.
multiplication, grouping and sharing	I made 7 groups of 4. There are 28 in total.		$12 \div \boxed{= 3}$ $x 3 = 12$ $x 3 = 12$ $x 3 = 12$ $x 3$
	<i>I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.</i>	$60 \div 4 = 15$ $60 \div 15 = 4$	Understand missing number problems for

	I have 28 in total. I made groups of 4. There are 7 equal groups.		division calculations and know how to solve them using inverse operations. $22 \div ? = 2$ $22 \div 2 = ?$ $? \div 2 = 22$ $? \div 2 = 22$
Dividing whole numbers by 10, 100 and 1,000	Use place value equipment to support unitising for division. $4,000 \div 1,000$ $4,000 \times 1,000$ 4,000 is 4 thousands. $4 \times 1,000 = 4,000$ So, $4,000 \div 1,000 = 4$	Use a bar model to support dividing by unitising. $380 \div 10 = 38$ 380 7 7 7 7 7 7 7 7	Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
Dividing by multiples of 10, 100 and 1,000	Use place value equipment to represent known facts and unitising. Use place value equipment to represent known facts and unitising. Use place value equipment to represent to represent to the set of the set	Represent related facts with place value equipment when dividing by unitising.	Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check. $3,000 \div 5 = 600$ $3,000 \div 500 = 60$ $5 \times 600 = 3,000$ $50 \times 60 = 3,000$ $500 \times 6 = 3,000$

		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
Dividing up to four digits by a single digit using short division	Explore grouping using place value equipment. 268 ÷ 2 = ? There is 1 group of 2 hundreds. There are 3 groups of 2 tens. There are 4 groups of 2 ones. 264 ÷ 2 = 134	<ul> <li>Use place value equipment on a place value grid alongside short division. The model uses grouping. A sharing model can also be used, although the model would need adapting.</li> <li>4 4 8 • • • • • • • • • • • • • • • • •</li></ul>	Use short division for up to 4-digit numbers divided by a single digit. $\begin{array}{r} 0 & 5 & 5 & 6 \\ 7 & 3 & ^3 8 & ^3 q & ^4 2 \end{array}$ $3,892 \div 7 = 556$ Use multiplication to check. $556 \times 7 = ?$ $6 \times 7 = 42$ $50 \times 7 = 350$ $500 \times 7 = 3500$ 3,500 + 350 + 42 = 3,892

		4       9       2       T       0       First, lay out the problem.         4       9       2       T       0       into 9 tens?         4       9       2       T       0       into 9 tens?         2       groups of 4 tens with 1 ten left over.       Exchange the 1 ten left over for 10 ones.         4       9       12       T       0         4       9       12       T       0         4       9       12       T       0         6       6       6       6       0         4       9       12       T       0         6       6       6       6       6         6       6       6       6       6         6       6       6       6       6         7       0       6       6       6         6       6       6       6       6         7       0       6       6       6         7       0       6       6       6         7       0       6       6       6         7       0       6       6       6         <	
Understanding remainders	Understand remainders using concrete versions of a problem. 80 cakes divided into trays of 6. 80 cakes in total. They make 13 groups of 6, with 2 remaining.	Use short division and understand remainders as the last remaining 1s. $\begin{bmatrix} 1 \\ 8 \\ 0 \end{bmatrix} \xrightarrow{T} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\$	In problem solving contexts, represent divisions including remainders with a bar model. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Dividing decimals by 10, 100 and 1,000	Understand division by 10 using exchange. 2 ones are 20 tenths. 20 tenths divided by 10 is 2 tenths.	Represent division using exchange on a place value grid.	Understand the movement of digits on a place value grid.

		$\circ$ TthHth $\circ$ $\circ$ Tth $\bullet$ $\circ$	$0.85 \div 10 = 0.085$ $0 \bullet 10 + 10 + 10 + 10 + 10 + 10 + 10 + 1$
Understanding the relationship between fractions and division	Use sharing to explore the link between fractions and division. <i>1 whole shared between 3 people.</i> <i>Each person receives one-third.</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>()</i> <i>(</i>	Use a bar model and other fraction representations to show the link between fractions and division. $I \div 3 = \frac{1}{3}$	Use the link between division and fractions to calculate divisions. $5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$ $11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$
		Year 6	
	Concrete	Pictorial	Abstract
Year 6 Addition			

Comparing and selecting efficient methods	Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.	Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations. $\underbrace{+3.00 + 500 + 20 + 20 + 2}_{40.265} + \underbrace{+20 + 2}_{40.265} + \underbrace{+20 + 2}_{40.265} + \underbrace{+20 + 2}_{40.265} + \underbrace{+20 + 2}_{40.265} + \underbrace{+3.500 + 2}_{40.265} + \underbrace{+1.500 + 2}_{40.265} +$	Use column addition where mental methods are not efficient. Recognise common errors with column addition. $32,145 + 4,302 = ?$ $\frac{\text{TTh Th } \text{H } \text{T } \text{O}}{3 \ 2 \ 1 \ 4 \ 5} + \frac{4 \ 3 \ 0 \ 2}{3 \ 6 \ 4 \ 4 \ 7} + \frac{4 \ 3 \ 0 \ 2}{7 \ 5 \ 1 \ 6 \ 5}$ $Which method has been completedaccurately? What mistake has been made? Column methods are also used for decimaladditions where mental methods are notefficient. \frac{\text{H } \text{T } \text{O} \cdot \text{Tth } \text{Hth}}{1 \ 4 \ 0 \ 0 \ 9} + \frac{4 \ 9 \ 8 \ 9}{1 \ 8 \ 9 \ 9 \ 8} = \frac{1}{1}$
Selecting mental methods for larger numbers where appropriate	Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods. $\underbrace{M  HTh  TTh  Th  H  T  0}_{2,411,301 + 500,000 = ?}$ This would be 5 more counters in the HTh place.	Use a bar model to support thinking in addition problems. 257,000 + 99,000 = ? ? $f_{257,000}$ $f_{100,000}$ <i>I added 100 thousands then subtracted</i> <i>1 thousand.</i>	Use place value and unitising to support mental calculations with larger numbers. 195,000 + 6,000 = ? 195 + 5 + 1 = 201 195 thousands + 6 thousands = 201 thousands So, 195,000 + 6,000 = 201,000

	So, the total is 2,911,301. 2,411,301 + 500,000 = 2,911,301	257 thousands + 100 thousands = 357 thousands 257,000 + 100,000 = 357,000 357,000 - 1,000 = 356,000 So, 257,000 + 99,000 = 356,000	
Understanding order of operations in calculations	Use equipment to model different interpretations of a calculation with more than one operation. Explore different results. $3 \times 5 - 2 = ?$	Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations. $\begin{bmatrix} 16 \times 4 \\ \\ 16 \times 4 \\ \\ 16 \times 6 \end{bmatrix} = ?$ $\begin{bmatrix} 16 \times 4 \\ \\ 44 + 4 + 4 + 4 + 4 + 4 + 4 + 4 + $	Understand the correct order of operations in calculations without brackets. Understand how brackets affect the order of operations in a calculation. $4 + 6 \times 16$ 4 + 96 = 100 $(4 + 6) \times 16$ $10 \times 16 = 160$
Year 6 Subtraction			
Comparing and selecting efficient methods	Use counters on a place value grid to represent subtractions of larger numbers.	Compare subtraction methods alongside place value representations. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy. $\frac{Th}{1} \frac{H}{8\pi} \frac{T}{10} \frac{O}{12} = \frac{+6}{1.552} \frac{-400}{1.552} \frac{+6}{1.552} \frac{-400}{1.552}$ Use column subtraction for decimal problems, including in the context of

		Use a bar model to represent calculations, including 'find the difference' with two bars as comparison. $\underbrace{\text{computer game}}_{\text{puzzle book}} \xleftarrow{\text{fl}_{2\cdot50}}$	H       T       O       · Tth Hth         3       0       9       · 6       0         -       2       0       6       · 4       0         1       0       3       · 2       0
Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations. 950,000 - 150,000 That is 950 thousands - 150 thousands $950 \leftrightarrow 800$ So, the difference is 800 thousands. 950,000 - 150,000 = 800,000	Subtract efficiently from powers of 10. 10,000 - 500 = ?
Year 6 Multiplication			
Multiplying up to a 4-digit number by a single digit number	Use equipment to explore multiplications. $\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Use place value equipment to compare methods. Method I	Understand area model and short multiplication. Compare and select appropriate methods for specific multiplications. Method 3 $3,000 \ 200 \ 20 \ 5$ $4 \ 12,000 \ 800 \ 80 \ 20$ 12,000 + 800 + 80 + 20 = 12,900 Method 4 $3 \ 2 \ 2 \ 5$ $\times \ 4 \ 1 \ 2 \ 9 \ 0 \ 0 \ 1 \ 2}$

Multiplying up to a 4-digit number by a 2-digit number		Use an area model alongside written multiplication. Method I 1,000  200  30  5 20 $20,000  4,000  600  100$ 1 $1,000  200  30  5$ $\times  2  1$ $5  1 \times 5$ $3  0  1 \times 30$ $2  0  0  1 \times 1000$ $1  0  0  20 \times 5$ $6  0  0  20 \times 30$ $4  0  0  0  20 \times 200$ $2  0  0  0  20 \times 1000$ 2  5  9  3  5	Use compact column multiplication with understanding of place value at all stages.
Using knowledge of factors and partitions to compare methods for multiplications	Use equipment to understand square numbers and cube numbers. $5 \times 5 = 5^2 = 25$ $5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$	Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.	Use a known fact to generate families of related facts. $\begin{array}{c} 170 \times 11 \\ 170 \times 12 \end{array}$ $\begin{array}{c} 171 \times 11 \\ 171 \times 11 \end{array}$ $\begin{array}{c} 171 \times 11 \\ 171 \times 110 \end{array}$ Use factors to calculate efficiently. $\begin{array}{c} 15 \times 16 \\ = 3 \times 5 \times 2 \times 8 \\ = 3 \times 8 \times 2 \times 5 \\ = 24 \times 10 \\ = 240 \end{array}$
Multiplying by 10, 100 and	Use place value equipment to explore exchange in decimal multiplication.	Understand how the exchange affects decimal numbers on a place value grid.	Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100

1,000	TorusticTorusticRepresent 0.3.TorusticMultiply by 10.Exchange each group of ten tenths. $0.3 \times 10 = ?$ $0.3$ is 3 tenths. $10 \times 3$ tenths are 30 tenths. $30$ tenths are equivalent to 3 ones.	$T \xrightarrow{0} \cdot Tth$ $T \xrightarrow{0} \cdot Tth$ $T \xrightarrow{0} \cdot Tth$ $T \xrightarrow{0} \cdot Tth$ $3 \xrightarrow{3} \cdot T$ $0 \cdot 3 \times 10 = 3$	and 1,000. $8 \times 100 = 800$ $8 \times 300 = 800 \times 3$ = 2,400 $2 \cdot 5 \times 10 = 25$ $2 \cdot 5 \times 20 = 2 \cdot 5 \times 10 \times 2$ = 50
Multiplying decimals	Explore decimal multiplications using place value equipment and in the context of measures. $\begin{array}{cccccccccccccccccccccccccccccccccccc$	Represent calculations on a place value grid. $3 \times 3 = 9$ $3 \times 0.3 = 0.9$ TOOTH 0000 0000 Understand the link between multiplying decimals and repeated addition. TOOTH 00000 0000 0000 0000 0000 00000 00000 00000 00000 00000 00000 00000 00000 00000 00000 00000 00000 000000 000000 000000	Use known facts to multiply decimals. $4 \times 3 = 12$ $4 \times 0.3 = 1.2$ $4 \times 0.03 = 0.12$ $20 \times 5 = 100$ $20 \times 0.5 = 10$ $20 \times 0.05 = 1$ Find families of facts from a known multiplication. I know that $18 \times 4 = 72$ . This can help me work out: $1.8 \times 4 = ?$ $18 \times 0.4 = ?$ $18 \times 0.4 = ?$ $18 \times 0.04 = ?$ Use a place value grid to understand the effects of multiplying decimals.

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			2 × 3 6 •
			0·2 × 3 0 • 6
			0·02 × 3
Year 6 Division			
Understanding factors	Use equipment to explore different factors of a number.	Recognise prime numbers as numbers having exactly two factors. Understand the link with division and remainders.	Recognise and know primes up to 100. Understand that 2 is the only even prime, and that 1 is not a prime number.
	$24 \div 4 = 6$ $30 \div 4 = 7 \text{ remainder } 2$ 4 is a factor of 24 but is not a factor of 30.	I7÷2=8r1       I7÷3=5r2       I7÷4=4r1       I7÷5=3r2	I       2       3       4       5       6       7       8       9       10         II       I2       I3       I4       I5       I6       17       I8       19       20         21       22       23       24       25       26       27       28       29       30
Dividing by a single digit	Use equipment to make groups from a total.	H T O B B C C C C C C C C C C C C C C C C C C	Use short division to divide by a single digit. $_{0}$
		$H \qquad T \qquad O  Grave Grav$	6 1 3 2 0 2
	There are 78 in total. There are 6 groups of 13. There are 13 groups of 6.	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	6 1 3 12
	There are is groups or o.		0 2 2 6 1 3 2
			Use an area model to link multiplication and division.

Dividing by a 2-digit number using factors	Understand that division by factors can be used when dividing by a number that is not prime.	Use factors and repeated division. $1,260 \div 14 = ?$ $1,260 \div 2 = 630$ $630 \div 7 = 90$ $1,260 \div 14 = 90$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Dividing by a 2-digit number using long division	Use equipment to build numbers from groups.	Use an area model alongside written division to model the process. $377 \div 13 = ?$ $377 \div 13 = ?$ $377 \div 13 = ?$ $377 \div 13 = 29$	Use long division where factors are not useful (for example, when dividing by a 2-digit prime number). Write the required multiples to support the division process. $377 \div 13 = ?$ 13 3 7 7 $- \frac{1}{3} \frac{3}{0} \frac{7}{7}$ $- \frac{1}{3} \frac{3}{0} \frac{10}{24} \frac{10}{7}$ $- \frac{1}{0} \frac{3}{2} \frac{0}{2} \frac{10}{2}$

100 and 1,000	Use place value equipment to explore division as exchange.	Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid. $\frac{12}{1+2} + 2 \times 10 = 12$ Understand how to divide using division by 10, 100 and 1,000. $12 \div 20 = ?$	377 ÷ 13 = 29 A slightly different layout may be used, with the division completed above rather than at the side. 21 $\boxed{7 + 9 + 8} = -\frac{6}{6} + \frac{3}{6} $
decimals	division of decimals.		to 2 decimal places.

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8 tenths divided into 4 groups. 2 tenths in each group.	$0.8$ ?       ?       ? $4 \times 2 = 8$ $8 \div 4 = 2$ So, $4 \times 0.2 = 0.8$ $0.8 \div 4 = 0.2$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
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